DOCUMENT RESUME

ED 317 432 SE 051 351

AUTHOR Blum-Anderson, Judy

TITLE Affect and Mathematics: Persistence in the

Mathematical Environment.

PUB DATE 89

NOTE llp.; Paper presented at the Conference on Women in

Mathematics and Sciences (St. Cloud University, MN,

November 10-11, 1989).

PUB TYPE Viewpoints (120) -- Speeches/Conference Papers (150)

EDRS PRICE M Ol/PCO1 Plus Postage.

DESCRIPTORS *Affective Behavior; Enrollment Influences; Females;

Intervention; Junior High Schools; Mathematics
Education; *Minority Groups; Secondary Education;
*Secondary School Mathematics; Sex Differences; *Sex

Stereotypes; *Student Attitudes

ABSTRACT

The attitudes and beliefs that students hold about the subject of mathematics and about themselves as learners of mathematics contribute as much to the school's mathematical environment as do the concrete and cognitive aspects of mathematics. This paper considers the effects of mathematical affect and the use of intervention programs to increase the retention of women and minorities in higher-level mathematics courses. Mathematical affect plays a role in the development of long-term mathematical persistence behaviors, such as course-enrollment decisions. The most critical period in which to use interventions to influence mathematical affect is the middle/junior high school age level. More students will be able to develop the short-term persistence behaviors necessary to experience success within the mathematical environment when attention to affect begins to be included as a regular part of the mathematics curriculum. Once students possess short-term persistence behaviors, it will be easier to motivate them to continue to enroll in mathematics courses. (YP)

Reproductions supplied by EDRS are the best that can be made



AFFECT AND MATHEMATICS:

PERSISTENCE IN THE MATHEMATICAL ENVIRONMENT

PERMISSION TO REPRODUCE THIS MATERIAL HAS BEEN GRANTED BY

TO THE EDUCATIONAL RESOURCES INFORMATION CENTER (ERIC)."

U.S. DEPARTMENT OF EDUCATION
Citicle of Educational Research and improvement
EDUCATIONAL RESOURCES INFORMATION
CENTER (ERIC)
This document has been reproduced as received from the person of organization
Originating of Minor changes have been made to improve reproduction quality.

Prints of view or opinions stated in this dox ument do not necessarily represent official OFRI position or policy

Judy Blum-Anderson, Ph.D. Candidate Washington State University November 1989

Paper prepared for discussion at the "Conference on Women in Mathematics and the Sciences," St. Cloud State University, Nov. 10–11, 1989.

158 150 A PR

AFFECT AND MATHEMATICS: PERSISTENCE IN THE MATHEMATICAL ENVIRONMENT

The components of a school's mathematical environment consist of much more than pages of textbooks, mathematical achievement test scores, and grade reports; the students are a major part of that environment. The attitudes and beliefs that students hold about the subject of mathematics and about themselves as learners of mathematics contribute as much to that environment as do the concrete and cognitive aspects of mathematics. It is not likely that students will be highly motivated to persist in the study of mathematics if little attention is given to the development of their attitudes and beliefs about mathematics (their mathematical affect). A mathematical environment cannot be considered to be healthy if any one of its individual components is not functioning to its potential.

Healthy mathematical environments have enrollment patterns in upper-division courses that include equal numbers of male and female students from all levels of the school's achievement range. Traditionally, participation in higher-level mathematics courses has been heavily weighted towards white males who occupy not only the majority of the



seats in the higher-level mathematics classrooms but, in turn, hold the majority of the positions in economically-rewarding professions which required higher-level mathematics in order to gain entrance to those professions.

When students fail to develop the persistence behaviors that are necessary in order for them to continue to enroll in higher-level mathematics courses, they are effectively filtering themselves out of complete freedom of educational and occupational choice (Davis & Hersh, 1986; Wiggans et al., 1983; Sells, 1978). Some examples of the filtering effects of mathematics are when employers use scores from standardized mathematical tests as quick and easy ways to screen job applications even if the ability to perform mathematical operations is not part of the actual job requirements, and when some graduate schools of business use a calculus requirement as an inexpensive way of screening out applicants when the number of applications exceeds the number of spaces available (Davis & Hersh, 1986). When mathematics scores are used to screen applications, the consequence is that the applications from women and minorities are the ones that are most often eliminated.

Recent research on gender-related differences and mathematics achievement indicates that while there are few gender-related



differences in cognitive mathematical achievement when the amount and type of mathematics taken is controlled (Smith & Walker, 1988), there are consistent and significant differences between the sexes in several affective areas (Reyes, 1984; Fennema & Sherman, 1977). Additionally, gender-related differences in mathematical affect exist even when there is no evidence of differences in achievement (Fennema, 1985). It appears that it might be likely that the differential mathematical course-taking behaviors that are found between females and males are more dependent upon affective, socio-cultural factors instead of differences in cognitive abilities (Eccles & Jacobs, 1986; Day, Langbort, & Skolnick, 1982; Fennema & Sherman, 1977).

Mathematical Affect

Schemas related to mathematical affect are constructed by students during interactions with mathematical concepts within the confines of formal mathematical environments. The nature of the affective components of each students' mathematical schemata influences whether or not students will develop short-term and long-term persistence behaviors in the study of mathematics (Marshall, 1989). Affective schemas hypothesized to be the most influential in the development of



mathematical persistence are those which are related to a belief in the usefulness of mathematics, confidence in the ability to learn mathematics, and attributional style (Fennema & Peterson, 1985). No single affective variable, alone, will determine whether or not a student will persist in the study of mathematics.

Positive mathematical affect can assist students in bringing routine and nonroutine problems to completion; however, negative mathematical affect can serve to scramble or even arrest cognitive processes and prohibit selection of appropriate completion strategies (Goleman, 1985; Isen, Daubman, & Gorgolione, 1987). Students demonstrate short-term persistence behaviors by having the ability to delay and become temporarily removed from the situation when emotions (negative affect) begin to interfere with cognition (Mandler, 1984, 1989), by developing an attributional style where failures are attributed to controllable factors (i.e. the applications of erroneous strategies or lack of effort) rather than to the uncontrollable factor of lack of ability (Weiner, 1986), and by recognizing that frustration is a normal part of learning mathematics (McLeod, 1988).

Mathematical affect plays a great role in the development of longterm mathematical persistence behaviors. These behaviors are



demonstrated at the time of course-enrollment decisions. Long-term mathematical persistence behaviors are influenced, in part, by the dictates of one's cultural reference group (Weiner, 1986; Mandler, 1984), by the sense of self-worth that one gains from participation in the activity in question (Covington, 1984), and by the information that one possesses with regard to the personal value that engagement in the activity will bring (Weiner, 1986; Maehr, 1984).

Influencing Mathematical Affect

Research has shown that affective variables leading to persistence in mathematical environments can be influenced by using intervention programs (Fennema, Wolleat, Pedro & Becker, 1981; Casserly, 1980; Brush, 1980). The use of mathematical intervention programs which highlight affective variables has resulted in increases in enrollment and/or in intentions to enroll in higher-level mathematics courses. The most critical period in which to use intervention to influence mathematical affect is the middle/junior high school age level. During this period, sextyping is at its peak and the school culture indicates that mathematics is becoming more difficult (Center for Early Adolescence, 1984; Casserly, 1980). Females and males possess nearly identical attitudes towards



mathematics during middle/junior high school; it is not until high school that the beliefs of males and females differ substantially, and enrollment patterns begin to favor males (Armstrong, 1980). High school is often too late to influence mathematical affect. It is nearly impossible to motivate students to return to the mathematics classroom after they have already elected to opt out of the mathematical sequence (Center for Early Adolescence, 1984).

Although research has shown that one-shot intervertion programs can be used to motivate students, in particular females and minorities, to desire to persist in the study of mathematics, it is not likely that the number of female and minority students taking higher-level mathematics courses can be substantially increased unless attention to affective issues is included as a regular component of the mathematical environment. When attention to affect begins to be included as a regular part of the mathematics curriculum, more students will be able to develop the short-term persistence behaviors that are necessary to experience success within the mathematical environment. When students possess short-term persistence behaviors with regard to mathematics, it will be easier to motivate them to continue to enroll in mathematics courses throughout their high school and college years.



REFERENCES

- Armstrong, J. (1980). <u>Achievement and participation of women in</u> <u>mathematics</u>: <u>An overview</u>. Denver: Education Commission of the States.
- Blum-Anderson, J. (in progress). Persistence motivation in a mathematical environment: Theory into practice. (Doctoral dissertation, Washington State University).
- Brush, L. (1980). <u>Encouraging girls in mathematics</u>: <u>The problem and the solution</u>. Massachusetts: Abt Books.
- Casserly, P. (1980). Factors affecting female participation in advanced placement programs in mathematics, chemistry and physics. In L. Fox, L. Brody & D. Tobin (Eds.), <u>Women and the mathematical mystique</u> (pp. 138–163). Baltimore: The Johns Hopkins University Press.
- Center for Early Adolescence. (1984). <u>Issues in middle-grade education:</u>
 <u>Girls, math and science</u> (NIE-G-84-0002). Carrboro, NC: University of North Carolina.
- Covington, M. (1984). The motive for self-worth. In R. Ames & C. Ames (Eds.), Research on motivation in education (pp. 77-113). Orlando: Academic Press.
- Day, L., Langbort, C., & Skolnick, J. (1982). How to encourage girls in math and science. Englewood Cliffs, NJ: Prentice-Hall.
- Davis, P., & Hersh, R. (1986). <u>Descartes' dream: The world according to mathematics</u>. Boston: Harcourt Brace Jovanovich.
- Eccles, J., & Jacobs, J. (1986). Social forces shape math attitudes and performance. <u>Signs</u>, <u>11</u>, 367-380.
- Fennema, E. (1985). Attribution theory and achievement in mathematics. In S. Yussen (Ed.), <u>The growth of reflection in young children</u> (pp. 245–265). New York: Academic Press.
- Fennema, E., & Peterson, P. (1985). Autonomous learning behavior: A



- possible explanation of gender-related differences in mathematics. In L. Wilkerson & C. Marrett (Eds.), <u>Gender influences in classroom interaction</u> (pp. 17-33). Orlando: Academic Press.
- Fennema, E., & Sherman, J. (1977). Sex-related differences in mathematics achievement, spatial visualization and affective factors. American Educational Research Journal, 14, 51-71.
- Fennema, E., Wolleat, P., Pedro, J., & Becker, A. (1981). Increasing women's participation in mathematics: An intervention study. <u>Journal for Research in Mathematics Education</u>, 12, 3-14.
- Goleman, D. (1985). <u>Vital lies, simple truths</u>. Simon and Schuster: New York.
- Isen, A., Daubman, K., & Gorgolione J. (1987). The influence of positive affect on cognitive organization: Implications for education. In R. Snow & M. Farr (Eds.), <u>Aptitude, Learning and Instruction</u> (pp. 35-75). Hillsdale, NJ: Lawrence Erlbaum Associates.
- Maehr, M. (1984). Meaning and motivation: Toward a theory of personal investment. In R. Ames & C. Ames (Eds.), <u>Research on motivation in education</u> (pp. 115–144). Orlando: Academic Press.
- Mandler, G. (1984). Mind and body: Psychology of emotion and stress. New York: W.W. Norton and Co.
- Mandler, G. (1989). Affect and learning: Reflections and prospects. In D. B. McLeod & V. Adams (Eds.), <u>Affect and mathematical problem solving:</u> <u>A new perspective</u> (pp. 3-19). New York: Springer-Verlag.
- Marshall, S. (1989). Affect in schema knowledge: Source and impact. In D.B. McLeod & V. Adams (Eds.), <u>Affect and mathematical problem</u> solving: A new perspective (pp. 49-58). New York: Springer-Verlag.
- McLeod, D. (1988, May). <u>Research on learning and instruction in</u> <u>mathematics</u>: <u>The role of affect</u>. Paper presented at "The First Wisconsin Symposium for Research on Teaching and Learning Mathematics," Madison, Wisconsin.



- Reyes, L. (1984). Affective variables and mathematics education. <u>The Elementary School Journal</u>, <u>84</u>, 558-581.
- Sells, L. (1978). Mathematics—a critical filter. The Science Teacher, 45, 28-29.
- Smith, S., & Walker, W. (1988). Sex differences on New York State regents examinations: Support for the differential course-taking hypothesis.

 <u>Journal for Research in Mathematics Education</u>, 19, 81-85.
- Weiner, B. (1986). An attributional theory of motivation and emotion. New York: Springer-Verlag.
- Wertime, R. (1979). Students, problems, and courage spans. In J. Lochhead & J. Clement (Eds.), <u>Cognitive Process Instruction</u> (pp. 191-199). Philadelphia: The Franklin Institute Press.
- Wiggans, L., Morris, M., Gamery, R., & Kryger, M. (1983). Math: Who needs it? (A report on Math Avoidance, Math Anxiety and Career Choices). Mathematics Department, Toronto Board of Education: Toronto, Canada.

